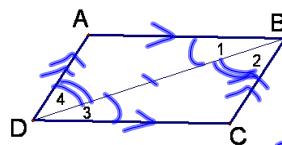
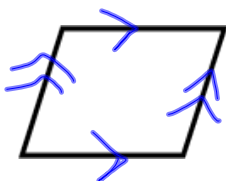


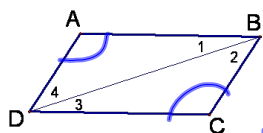
## 8-2 Parallelograms

Parallelogram-quadrilateral with both pairs of opposite sides parallel



Given:  $\square ABCD$   
 Prove:  $\overline{AB} \cong \overline{CD}$   
 $\overline{AD} \cong \overline{BC}$

- | S.                                                                                   | R.                       |
|--------------------------------------------------------------------------------------|--------------------------|
| ① $\square ABCD$                                                                     | ① Given                  |
| ② $\overline{AB} \parallel \overline{DC}$<br>$\overline{AD} \parallel \overline{BC}$ | ② def of $\square$       |
| ③ $\angle 1 \cong \angle 3$<br>$\angle 2 \cong \angle 4$                             | ③ Alt Int $\angle$ s thm |
| ④ $\overline{BD} \cong \overline{BD}$                                                | ④ Reflexive              |
| ⑤ $\triangle ABD \cong \triangle CDB$                                                | ⑤ ASA                    |
| ⑥ $\overline{AB} \cong \overline{CD}$<br>$\overline{AD} \cong \overline{BC}$         | ⑥ CPCTC                  |



Given:  $\square ABCD$   
 Prove:  $\angle A \cong \angle C$

- 
- ① - ⑤ from previous proof  
 ⑥  $\angle A \cong \angle C$  ⑥ CPCTC

Theorem 8.3-Opposite sides of a parallelogram are congruent

Opp sides  $\square \cong$

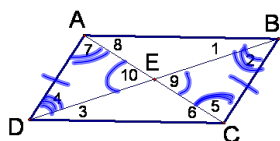


Theorem 8.4-Opposite angles of a parallelogram are congruent



Theorem 8.5-Consecutive angles of a parallelogram are supplementary

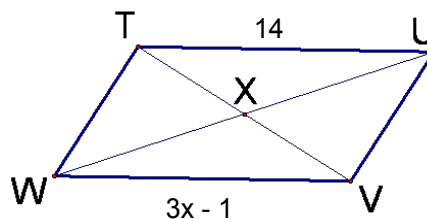
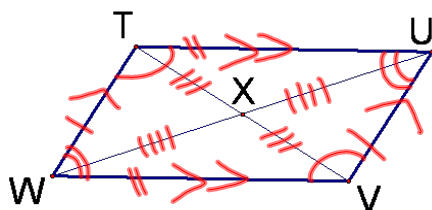
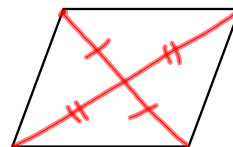




Given:  $\square ABCD$   
 Prove:  $\overline{AE} \cong \overline{CE}$   
 $\overline{DE} \cong \overline{BE}$

- | S-                                                                               | R                                |
|----------------------------------------------------------------------------------|----------------------------------|
| ① $\sim$                                                                         | ① Given                          |
| ② $\angle 10 \cong \angle 9$                                                     | ② Vert $\angle s \cong$          |
| ③ $\overline{AB} \parallel \overline{DC}; \overline{AD} \parallel \overline{BC}$ | ③ def of $\square$               |
| ④ $\angle 7 \cong \angle 5; \angle 4 \cong \angle 6$                             | ④ Alt Int $\angle s \text{ thm}$ |
| ⑤ $\overline{AD} \cong \overline{BC}$                                            | ⑤ Opp sides $\square are \cong$  |
| ⑥ $\triangle AED \cong \triangle CEB$                                            | ⑥ AAS                            |
| ⑦ $\overline{AE} \cong \overline{CE}$<br>$\overline{DE} \cong \overline{BE}$     | ⑦ CPCTC                          |

Theorem 8.6-Diagonals of a parallelogram bisect each other



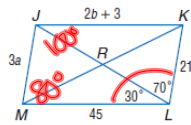
$$\begin{aligned} TX &= 8 \\ XV &= .5y \end{aligned}$$

$$\begin{aligned} 8 &= .5y \\ 16 &= y \end{aligned}$$

$$\begin{aligned} 3x - 1 &= 14 \\ 3x &= 15 \\ x &= 5 \end{aligned}$$

Use  $\square JKLM$  to find each measure or value if  $JK = 2b + 3$  and  $JM = 3a$ .

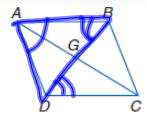
- |                  |                   |
|------------------|-------------------|
| 7. $m\angle MJK$ | 8. $m\angle JML$  |
| 9. $m\angle JKL$ | 10. $m\angle KJL$ |
| 11. $a$          | 12. $b$           |



Complete each statement about  $\square ABCD$ .

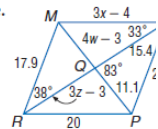
Justify your answer.

- |                                             |                                         |
|---------------------------------------------|-----------------------------------------|
| 16. $\angle DAB \cong \angle DCB$           | 17. $\angle ABD \cong \angle CDB$       |
| 18. $\overline{AB} \parallel \overline{CD}$ | 19. $\overline{BG} \cong \overline{EG}$ |
| 20. $\triangle ABD \cong \triangle CDB$     | 21. $\angle ACD \cong \angle CAB$       |



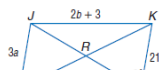
**ALGEBRA** Use  $\square MNPR$  to find each measure or value.

- |                   |                   |
|-------------------|-------------------|
| 22. $m\angle MNP$ | 23. $m\angle NRP$ |
| 24. $m\angle RNP$ | 25. $m\angle RMN$ |
| 26. $m\angle MQN$ | 27. $m\angle MQR$ |
| 28. $x$           | 29. $y$           |
| 30. $w$           | 31. $z$           |



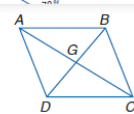
Use  $\square JKLM$  to find each measure or value if  $JK = 2b + 3$  and  $JM = 3a$ .

- |                  |                  |
|------------------|------------------|
| 7. $m\angle MJK$ | 8. $m\angle JML$ |
|------------------|------------------|



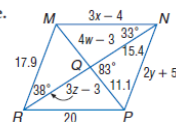
Complete each statement about  $\square ABCD$ . Justify your answer.

- |                                             |                                         |
|---------------------------------------------|-----------------------------------------|
| 16. $\angle DAB \cong \angle DCB$           | 17. $\angle ABD \cong \angle CDB$       |
| 18. $\overline{AB} \parallel \overline{CD}$ | 19. $\overline{BG} \cong \overline{EG}$ |
| 20. $\triangle ABD \cong \triangle CDB$     | 21. $\angle ACD \cong \angle CAB$       |



**ALGEBRA** Use  $\square MNPR$  to find each measure or value.

- |                   |                   |
|-------------------|-------------------|
| 22. $m\angle MNP$ | 23. $m\angle NRP$ |
| 24. $m\angle RNP$ | 25. $m\angle RMN$ |
| 26. $m\angle MQN$ | 27. $m\angle MQR$ |
| 28. $x$           | 29. $y$           |
| 30. $w$           | 31. $z$           |

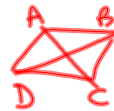


Find the point where the diagonals intersect.

ABCD is a parallelogram

A(5, -3) B(3, 5) C(-2, 7) D(0, -1)

Use midpt formula



$M(\frac{3}{2}, 2)$

HW  
p. 518-519  
3-16, 23-28,  
33-36